

Ionization Counter HW

#1- A beam of alpha particles produces a current of 10.14 A in a ionzation chamber for 8 s. The chamber contains air at STP ($W = 36 \text{ eV/ip}$). (ip - ion pair)

(a) How many ion pairs are produced?

$$n = Q/e = \frac{I\Delta t}{e} = (10.14A)(8s) / 1.6 \times 10^{-19} C = 5.07 \times 10^{20} \text{ ions}$$

(b) How much energy did the beam deposit in the chamber?

$$\Delta E = n W = (5.07 \times 10^{20}) 36 \text{ eV/ip} = 1.83 \times 10^{22} \text{ eV} = 2920 \text{ J}$$

(c) If the chamber volume is 240 cc, what is the energy absorbed per unit mass in units of gray (1 gray absorbed dose = 1 J/kg).

$$m_{\text{gas}} = \rho V = (1.297 \text{ kg} / 10^6 \text{ cc})(240 \text{ cc}) = 3.11 \times 10^{-4} \text{ kg}$$

$$\text{Absorbed Dose} = E / m(\text{kg}) = 2920 \text{ J} / 3.11 \times 10^{-4} \text{ kg} = 9.38 \times 10^6 \text{ G}$$

#2- A Po-210 (5.30 MeV) α source is placed in an air ionization chamber and a saturation current of $8 \times 10^{-12} \text{ A}$ is observed. Assuming the ionization is due to the aphas stopping in the chamber. How many stop per second?

$$N = \frac{\Delta E_{\alpha}}{W} = \frac{5.3 \times 10^6 \text{ eV} / \alpha}{36 \text{ eV}} = 1.47 \times 10^5 \text{ ip} / \alpha$$

$$\frac{dn}{dt} = \frac{1}{e} \frac{dq}{dt} = \frac{8 \times 10^{-12}}{1.6 \times 10^{-19}} = 5.0 \times 10^7 \text{ ip} / \text{s}$$

$$n_{\alpha} = \frac{1}{N} \frac{dn}{dt} = \frac{5.0 \times 10^7 \text{ ip} / \text{s}}{1.47 \times 10^5 \text{ ip} / \alpha} = 340 \alpha / \text{s}$$

#3. The oscilloscope pulse seen in a gas filled proportional chamber (gas gain 10^3) is 10 mV in pulse height and 20ns in pulse duration. The oscilloscope has a 50Ω input impedance. Determine the charge and number of ion pairs contained in the pulse.

$$q = \frac{1}{R} \int V(t) dt = \frac{1}{50\Omega} \left[\frac{1}{2} (0.010 \text{ V})(20 \times 10^{-9} \text{ s}) \right] = 2 \text{ pC}$$

1/2 base x height

$$n_e = \frac{2 \times 10^{-12} \text{ C}}{1.6 \times 10^{-19} \text{ C} / e} = 1.25 \times 10^7 = n_{\text{pair}} \times \text{gain}$$

$$n_{\text{pair}} = \frac{1.25 \times 10^7}{\text{gain}} = \frac{1.25 \times 10^7}{10^3} = 12,500$$

#4. Why is a GM counter not useful for determining the aborbed energy in a gas?

The charge released in a GM avalanche is not proportional to the incident energy.

#5. An argon filled GM tube counts a 30 keV X-ray source at a measured rate of $R_x = 100/\text{s}$. Using the efficiency ϵ curve from the X-ray Data Booklet, find the actual decay rate R_o of the source, where $R_x = R_o \times \epsilon$.

$$R_o = 100 \text{ s}^{-1} / 0.05 = 2000 \text{ s}^{-1} \quad \text{where } \epsilon \sim 0.05$$